

## Introduction

The Mathematics work your child is doing at school may look very different to the kind of 'sums' you remember.

This is because children are encouraged to work mentally, where possible, using personal jottings to help support their thinking. Number lines are one example of this.

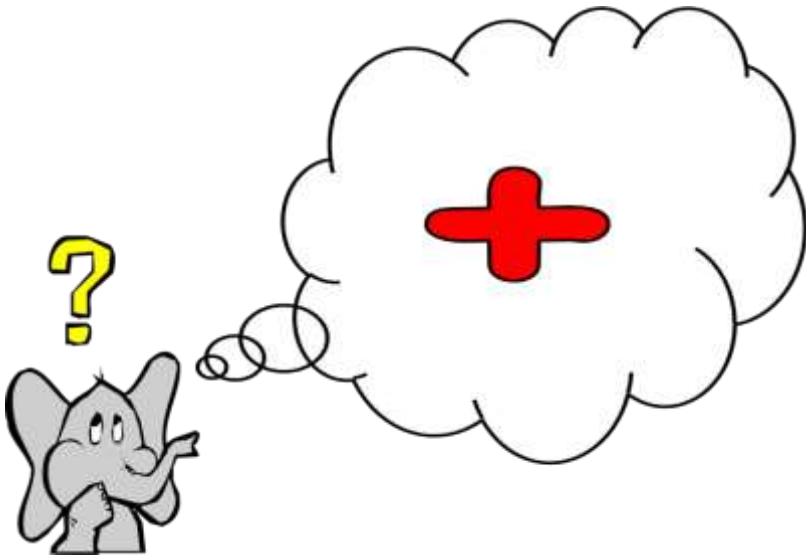
Even when children are taught more formal written methods they are only encouraged to use these methods for calculations they cannot solve in their heads.

It will be a great help to your child, and to their teachers, if you could encourage them to use methods which they have learnt at school rather than teaching them different methods at home.

This booklet is designed to inform

you about the progression through calculation methods that we use at Cranmore Infant School for addition, subtraction, multiplication and division. We have included the calculations that children learn in year 3. Some of our children will not be at that stage but we felt you would find it useful to see the whole process.

# Addition



add and count on  
addition plus  
more sum total  
altogether increase

FS2

Recognise numbers 0 to 10

012345678910

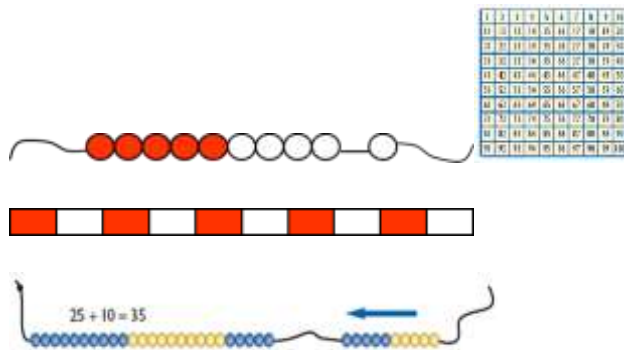
Count reliably up to 10 everyday objects



Find one more than a number



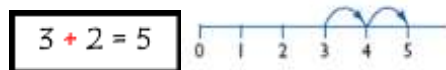
Count in ones and tens



Begin to relate addition to combining two groups of objects




Count along a number line to add numbers together



Begin to use the + and = signs to record

Children could draw a picture to help them work out the answer.

mental calculations in a number sentence

$6 + 4 = 10$  

Combining two sets of objects

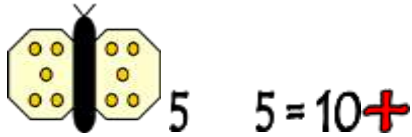
$2 + 3 = \square$

At a party, I eat 2 cakes and my friend eats 3. How many cakes did we eat altogether?

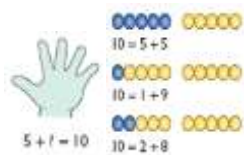
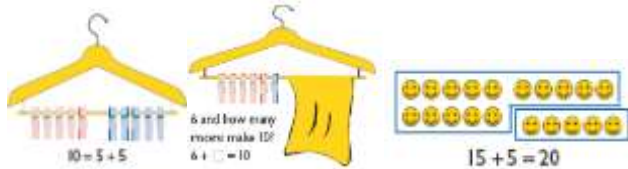
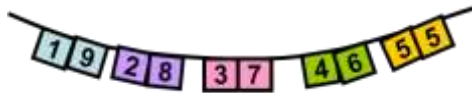


Y1


Know doubles of numbers



Know by heart all pairs of numbers with a total of 10 and 20

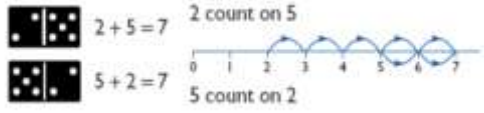


Know that addition can be done in any order

$1 + 2 = 3$   


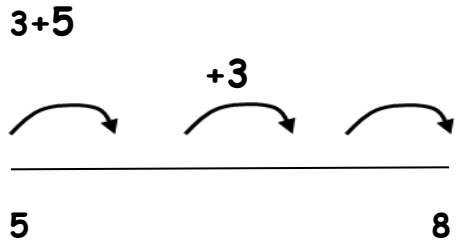
$2 + 1 = 3$   


Children could use dots or images to represent the numbers.



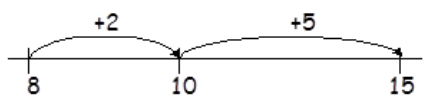
Put the biggest number first and

count on 

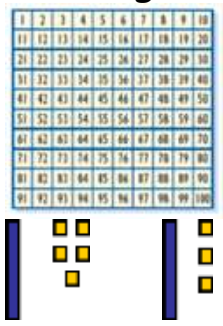


Add two single-digit numbers that bridge 10

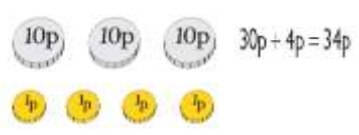
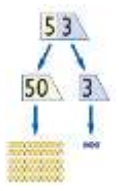
$8 + 7 = 15$



Counting on and back in 2,5,10's.



Begin to partition numbers in order to add.

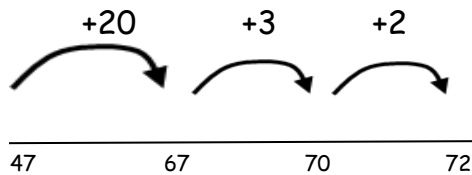
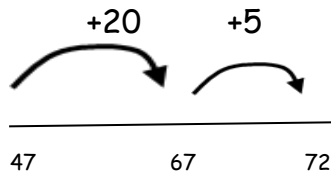
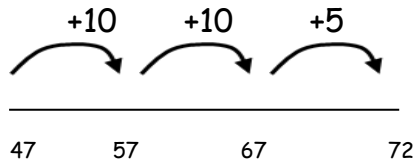


Understanding place value and using this to help add.

Y2

$$47 + 25 = \square$$

My sunflower is 47cm tall. It grows another 25cm. How tall is it now?



$$246 + 87$$

$$246 + 80 + 7 \quad \text{or} \quad 246 + 7 + 80$$

$$356 + 427 = 356 + (400 + 20 + 7)$$

**First steps**

$$356 + 400 = 756$$

$$756 + 20 = 776$$

$$776 + 7 = 783$$

**leading to:**

$$= 756 + 20 + 7$$

$$= 776 + 7$$

$$= 783$$

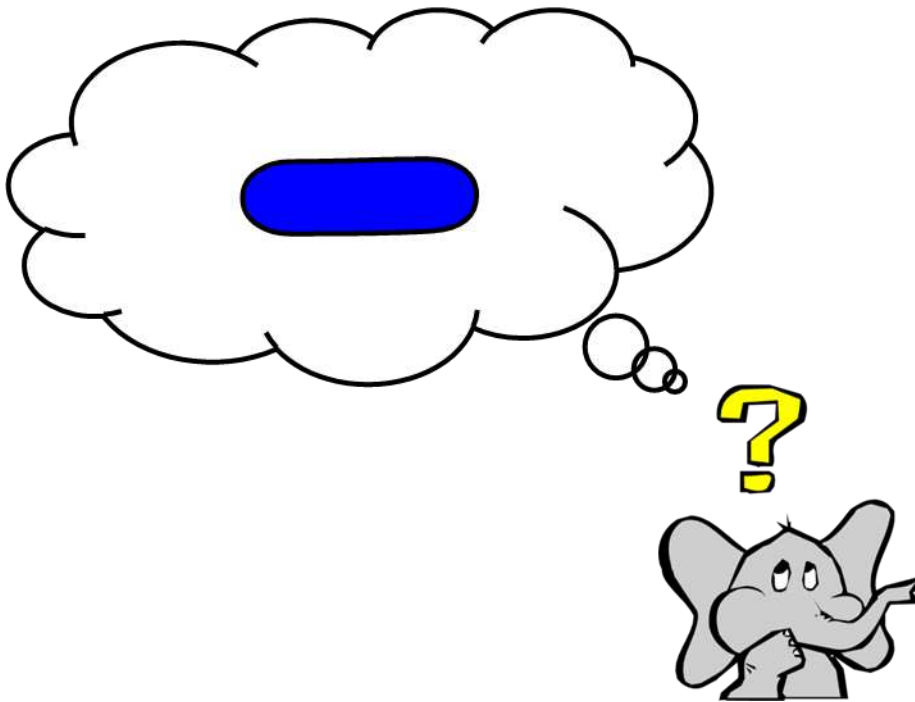
Drawing on a number line helps children to record the steps they have taken in a calculation (start on 47 + 10 + 10 then + 5). This is much more efficient than counting on in ones. They can progress to adding on in multiples of 10 (start at 47 + 20 then + 5).

Develop methods for adding two digit and three digit numbers by partitioning second number only.

<p>Y3</p>	<p>375+67= <input type="text"/></p> <p>300+70+5 60+7 300+130+12=442</p> <p><b>Leading to:</b></p> <table style="display: inline-table; vertical-align: top;"> <tr> <td>67</td> <td>83</td> </tr> <tr> <td>+ 24</td> <td>+42</td> </tr> <tr> <td>80</td> <td>120</td> </tr> <tr> <td>11</td> <td>5</td> </tr> <tr> <td>91</td> <td>125</td> </tr> </table> <div style="border: 1px solid black; padding: 5px; margin-top: 10px;"> <p>Add most significant digits first. Add mentally from top. This leads onto most significant digits first.</p> </div>	67	83	+ 24	+42	80	120	11	5	91	125	<p>Use knowledge of place value and partitioning of three digit numbers to develop written methods for addition of two and three digit numbers using expanded methods of recording.</p>
67	83											
+ 24	+42											
80	120											
11	5											
91	125											



# Subtraction



count back    take away

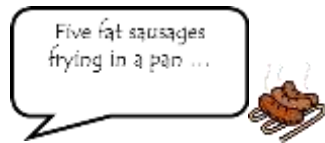
fewer    subtract

minus    less

difference between

FS2

Begin to count backwards in familiar contexts such as number rhymes or stories



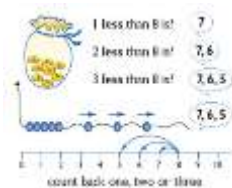
Continue the count back in ones from any given number.



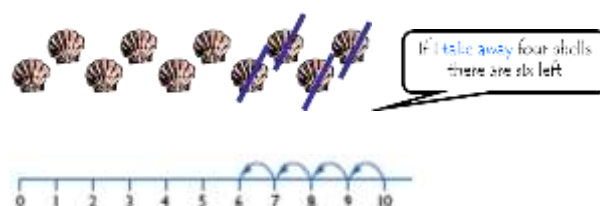
Begin to relate subtraction to 'taking away'



Find one less than a number



Count backwards along a number line to 'take away'



Drawing a picture helps children to visualise the problem.

$5-2= \square$

I had five balloons. Two burst. How many did I have left?



Take away

A teddy bear costs £5 and a doll costs £2. How much more does the bear cost?



Find the difference

Y1

Count back in tens

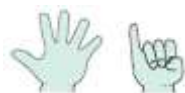


Begin to use the - and = signs to record mental calculations in a number sentence



$$6 - 4 = 2$$

Know by heart subtraction facts for numbers up to 10 and 20

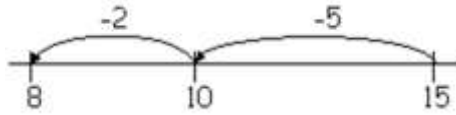


$$\begin{array}{l} 6 + 4 = 10 \\ 10 - 6 = 4 \end{array} \quad \begin{array}{l} 1 + 6 = 10 \\ 10 - 4 = 6 \end{array}$$

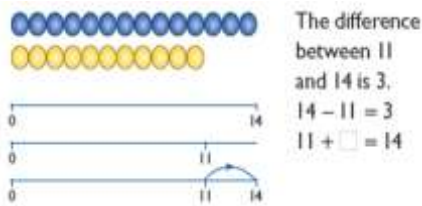
		$20 = 12 + 8$	$8 + 12 = 20$
		$20 - 8 = 12$	$20 - 12 = 8$

Subtract single digit numbers often bridging through 10

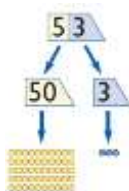
$$15 - 7 = 8$$



Begin to find the difference by counting up from the smallest number



Begin to partition numbers in order to take away



Understanding place value and using this to help add.

Y2

Subtract 10 from a two-digit number

$$45 - 10$$

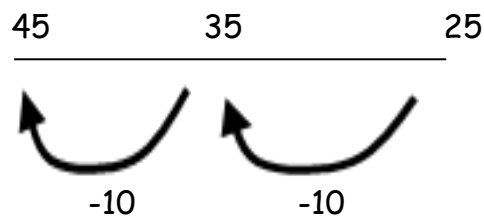
1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100



Subtract multiples of 10 from any number

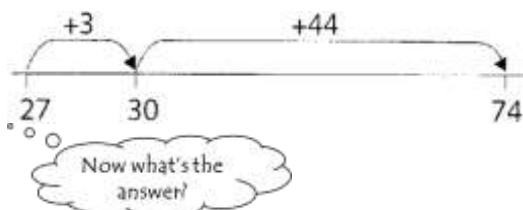
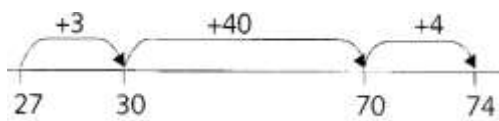
$$45 - 20$$

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100



Decide whether to count on or count back

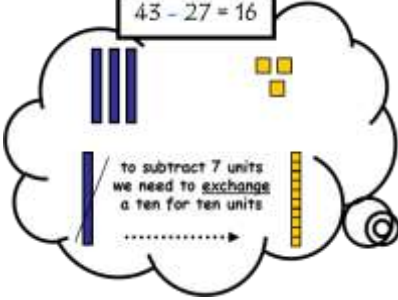






$$74 - 27 = 47$$



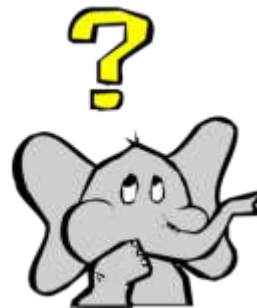
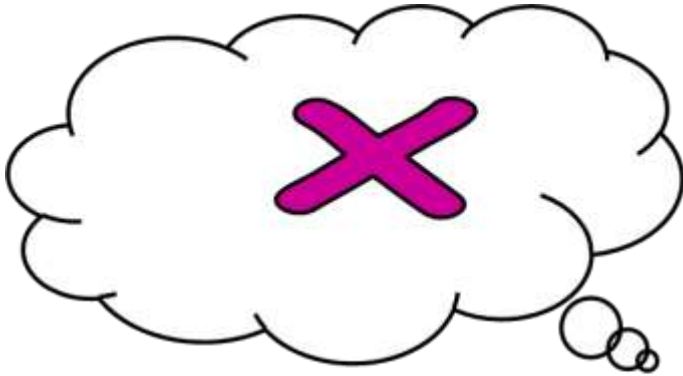
Expanded method

Begin to teach children about deciding to count on or back. Children could count on (from the smallest number to the biggest) using an empty number line. It is easiest to count up in multiples of 10.

It is important that the children have a good understanding of place value and partitioning using concrete resources and visual images to support

	<p style="text-align: center;"><math>43 - 27 = 16</math></p>  <table style="border-collapse: collapse; margin-left: auto; margin-right: auto;"> <tr> <td style="border-right: 1px solid black; padding: 5px; text-align: center;">T</td> <td style="padding: 5px;"></td> </tr> <tr> <td style="border-right: 1px solid black; padding: 5px; text-align: center;">  </td> <td style="padding: 5px; text-align: center;">  </td> </tr> <tr> <td style="border-right: 1px solid black; padding: 5px; text-align: center;">- 2</td> <td style="padding: 5px; text-align: center;">7</td> </tr> </table> <div style="border: 1px solid black; padding: 5px; width: fit-content; margin-left: auto; margin-right: auto;"> <math display="block">  \begin{array}{r}  \overset{30}{\cancel{40}} + \overset{10}{3} \\  - 20 + 7 \\  \hline  10 + 6  \end{array}  </math> </div>	T				- 2	7	<p>calculations. The expanded method enables children to see what happens to numbers in the standard written method.</p> <p>NOTE: the correct language is 'exchanges' not borrow.</p>
T								
								
- 2	7							
Y3	<p><b>Compact (short) written method</b></p> <div style="display: flex; justify-content: space-around; align-items: flex-start;"> <div style="border: 1px solid black; padding: 5px; margin: 5px;"> <math display="block">  \begin{array}{r}  \overset{30}{\cancel{40}} 13 \\  - 27 \\  \hline  16  \end{array}  </math> </div> <div style="border: 1px solid black; padding: 5px; margin: 5px;"> <math display="block">  \begin{array}{r}  432 \\  - 271 \\  \hline  161  \end{array}  </math> </div> </div> <div style="border: 1px solid black; padding: 5px; margin-left: auto; margin-right: auto;"> <math display="block">  \begin{array}{r}  43.2 \\  - 27.1 \\  \hline  16.1  \end{array}  </math> </div>	<p>The previous stages reinforce what happens to numbers when they are subtracted using more formal written methods. It is important that the children have a good understanding of place value and partitioning. This method can be used for larger numbers and decimals</p>						

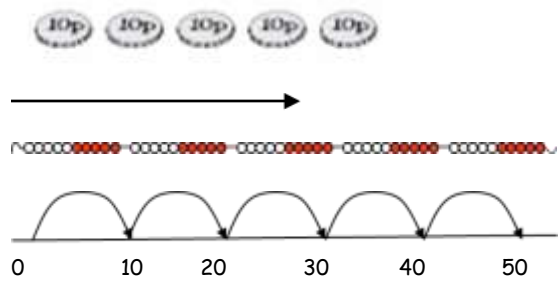
# Multiplication



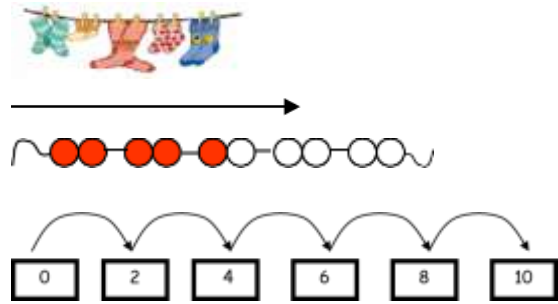
multiplication      product  
once, twice, three times  
double      groups of  
repeated addition      lots of  
array, row, column      multiply  
times      multiple

FS2

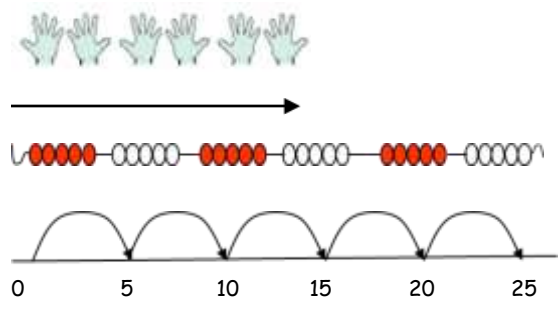
Count in tens from zero



Count in twos from zero



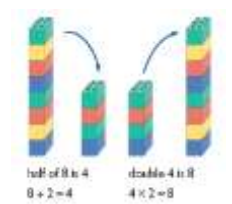
Count in fives from zero



Children are taught to understand multiplication as repeated addition and scaling. It can also describe an array.

Y1

Know doubles and corresponding halves

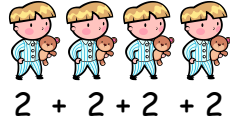


Knowing multiplication can be seen as repeat addition

Each child has two eyes. How many eyes do four children have?

Again a picture can be useful.





$4 \times 2 =$   
 4 lots of 2  
 4 groups of 2

$3 \times 5 =$

There are 5 cakes in a pack. How many cakes in 3 packs?

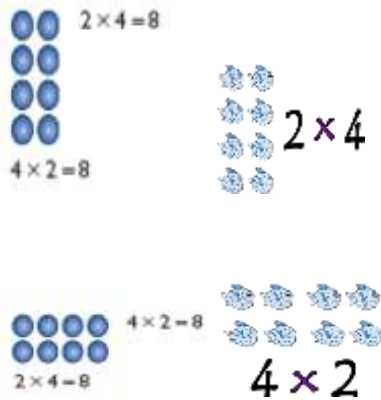
Dots or tally marks are often drawn in groups. This shows 3 lots of 5.

$5 + 5 + 5$



Understand multiplication as an array

Drawing an array (2 rows of 4 or 4 columns of 2) gives children an image of the answer. It also helps develop the understanding that  $4 \times 2$  is the same as  $2 \times 4$ .

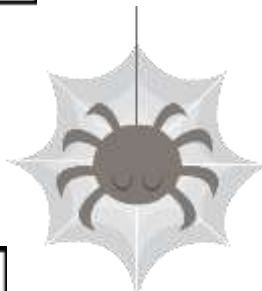


Y2

Know multiplication tables to  $10 \times 10$

$\times 5$

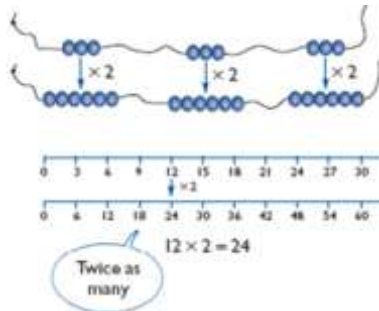
$3 \times 5 = 15$



$2 \times 5 = 10$

$8 \times 5 = 40$

$$6 \times 5 = 30$$



Use known facts to work out new ones

Use factors to multiply

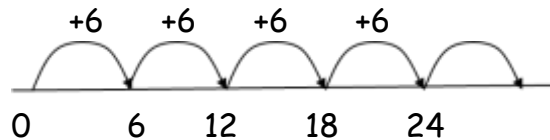
Understand that ...

$$24 \times 20 = 24 \times 2 \times 10$$

$$24 \times 50 = 24 \times 5 \times 10$$

$$4 \times 6 = \square$$

There are 4 cats. Each cat has 6 kittens. How many kittens are there altogether?

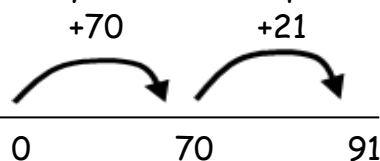


Children could count on in equal steps, recording each jump on an empty number line. This shows 4 jumps of 6.

Y3

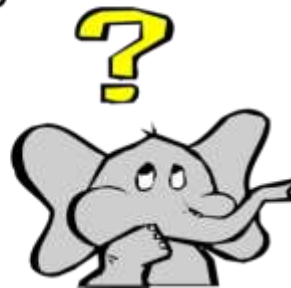
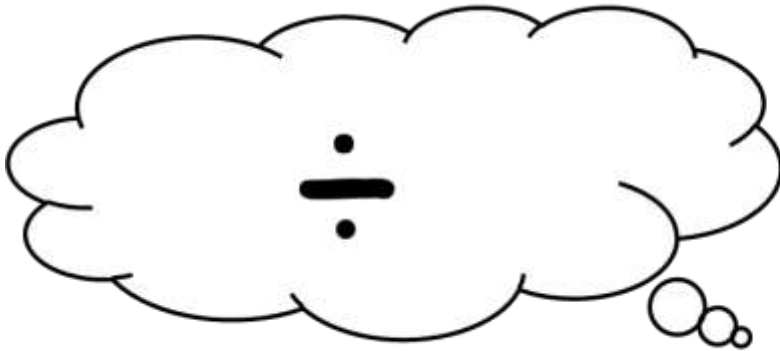
$$13 \times 7 = \square$$

There are 13 biscuits in a packet. How many biscuits in 7 packets?



When numbers get bigger it is inefficient to do lots of small jumps. Split 13 into parts (10 and 3). This gives you two jumps (10x7 and 3x7).

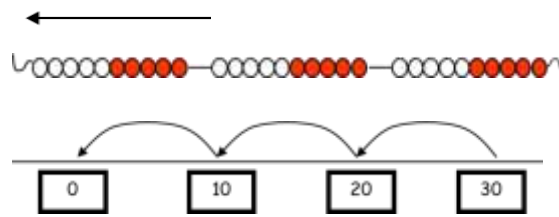
# Division



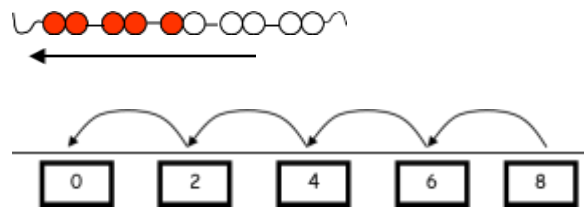
group                      groups of  
                                 lots of                      divide  
divided by  
division                      quotient                      factor  
                                 remainder                      divisible  
half                      halve                      share

FS2

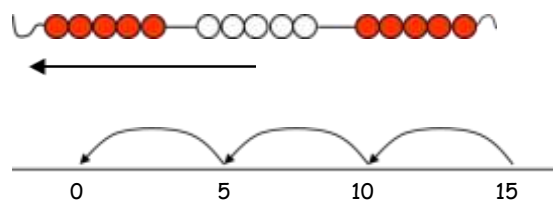
Count back in tens



Count back in twos

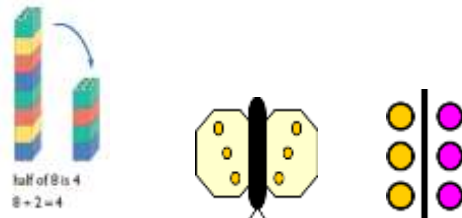


Count back in fives



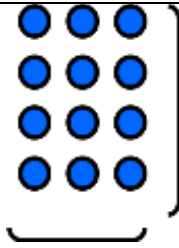
Y1

Know halves



Half of 6 is 3  
 $\frac{1}{2}$  of 6 = 3

Reinforce division as grouping through the use of arrays



12 divided into groups of 3 gives 4 groups  
 $12 \div 3 = 4$

12 divided into groups of 4 gives 3 groups  
 $12 \div 4 = 3$

Y2

Use known multiplication facts to work out corresponding division facts

If  $2 \times 10 = 20$

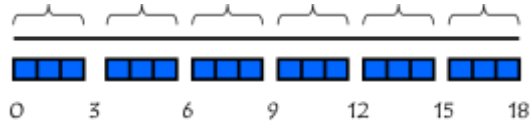
then

$20 \div 10 = 2$

$20 \div 2 = 10$

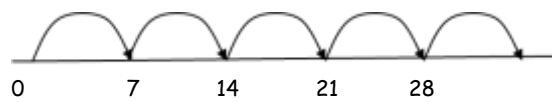
Represent 'groups' for division on a number line using apparatus alongside the line

18 divided into groups of 3  
 $18 \div 3 = 6$



$28 \div 7 = \square$

A chew bar costs 7p. How many can I buy with 28p?



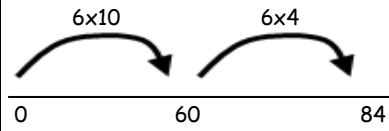
To work out how many 7's there are in 28, draw jumps of 7 along a number line. This shows you need 4 jumps of 7.

This can also be done starting from 28 and counting back in chunks of 7.

Y3

$$84 \div 6 = \square$$

I need 6 drawing pins to put up a picture. How many pictures can I put up with 84 pins?



It would take a long time to jump in sixes to 84 so children can jump on in bigger 'chunks'. A jump of 10 lots of 6 takes you to 60. Then you need another 4 lots of 6 to reach 84. Altogether, that is 14 sixes.